# Forecasting Patient Outcomes in Kidney Exchange

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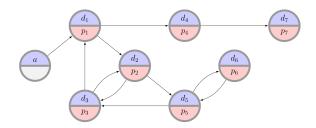
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**Table 13-2: OPTN KPD Prioritization Points** 

If the:	Then the match will receive:
Candidate is registered for the OPTN KPD program	.07 points for each day according to Policy 13.7.G: OPTN KPD Waiting Time Reinstatement
Candidate is a 0-ABDR mismatch with the potential donor	10 points
Transplant hospital that registered both the candidate and potential donor in the OPTN KPD program is the same	75 points
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Waiting times and odds of match can differ dramatically depending on a pair's features.

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Ideally, prediction is fast, only requires data accessible to the exchange, and gives confidence estimates.

#### A Simple Approach

We propose a simple random-forest approach to infer (O, W, Q) directly from the match record.

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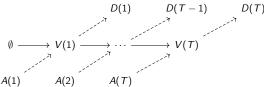
Can we predict (O, W, Q) for vertices  $v \sim f_P$  despite training on data for  $(v, O(v), W(v), Q(v)) \sim \mathcal{R}_T$ ?

Categorical	Donor/Patient Blood Type, Donor/Patient HLA		
Boolean	Donor/Patient Sex <sup>†</sup> , Donor Race, Donor Cigarette Use <sup>†</sup>		
Integer	Pool Size at Entry, Donor/Patient Age, Patient CPRA		
Float	Donor/Patient Weight <sup>‡</sup> , Donor eGFR <sup>‡</sup> , Donor BMI, Donor Systolic BP		

Data types of features used for prediction. Features with † are independently generated. Features with ‡ are conditionally generated. All other features are from real data.

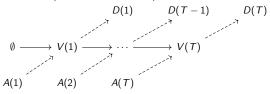
#### Simulation

**Batch Simulation** (up until time T) to obtain  $\mathcal{R}_T$ :



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**Trajectory Simulation** (run  $\tau$  times for S samples) to obtain the joint distribution of (v, O(v), W(v), Q(v)) for  $v \sim f_P$ :

$$V(T) \longrightarrow \mathbf{v}^* \in \mathbf{V}(\mathbf{T}+\mathbf{1}) \longrightarrow \mathbf{v}^* \in \mathbf{V}(\mathbf{T}^*) \longrightarrow V(T^*+\mathbf{1})$$

$$A(T+2) \qquad A(T^*)$$

#### Convergence of the Steady-State Constant

We measure the distance of the exchange to steady-state using the **steady-state constant** 

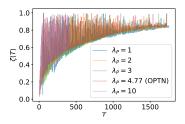
$$\zeta(T) := \frac{\left|\bigcup_{t=1}^{T} D(t)\right|}{\left|\bigcup_{t=1}^{T} A(t)\right|} = \frac{\sum_{t=1}^{T} |D(t)|}{\sum_{t=1}^{T} |A(t)|} = \frac{|\mathcal{R}_{T}|}{|\mathcal{R}_{T}| + |V(T)|} \in [0, 1]$$

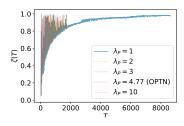
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No matter the size of the exchange, the constant empirically converges to 1!





#### Steady-State Implies Low Shift

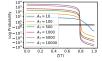
**Theorem.** Suppose each vertex  $\mathbf{v}_i \in \bigcup_{t=1}^T A(t)$  has features distributed as  $\mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$  where  $\boldsymbol{\Sigma}$  is full rank. Then,

$$\Pr\left[\mathcal{R}_{\mathcal{T}} \text{ is } (\gamma, \delta) \text{-shifted}\right] \leq \underbrace{\left(\frac{e}{1 - \zeta(\mathcal{T})}\right)^{A_{\mathcal{T}}(1 - \zeta(\mathcal{T}))}}_{\text{Number of coalitions}} \underbrace{\frac{e}{2^{\lceil \gamma d \rceil} \exp\left(-2A_{\mathcal{T}}\zeta(\mathcal{T})\lceil \gamma d \rceil \delta^2\right)}}_{2^{\lceil \gamma d \rceil} \exp\left(-2A_{\mathcal{T}}\zeta(\mathcal{T})\lceil \gamma d \rceil \delta^2\right)}$$

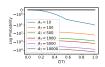
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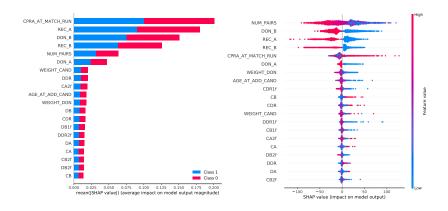
$$\gamma = \delta = 0.3, \ d = (10, 20, 30, 40)$$

#### Empirical Results in Realistic Simulations

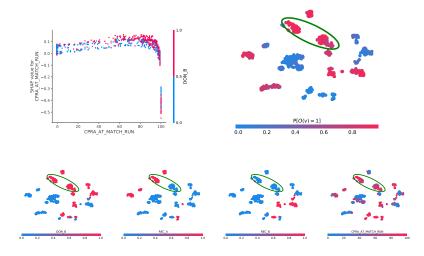
Arrival Rate	D	Federated	$ \mathcal{R}_{\mathcal{T}} $	ζ	$MAE(\widehat{O})$	$IOU\left(\widehat{W}_{95}\right)$	$IOU\left(\widehat{Q}_{95}\right)$
$\lambda_P = 1$	1500	No	56	0.397	0.258	0.451	0.747
$\lambda_P = 1$	4000	No	246	0.953	0.191	0.644	0.761
$\lambda_P = 1$	50000	No	4888	0.984	0.130	0.653	0.632
$\lambda_P = 2$	1500	No	157	0.477	0.221	0.336	0.815
$\lambda_P = 2$	4000	No	752	0.882	0.212	0.620	0.809
$\lambda_P = 3$	1500	No	285	0.523	0.184	0.386	0.798
$\lambda_P \approx 4.77 \text{ (OPTN)}$	1500	No	593	0.509	0.164	0.503	0.812
$\lambda_P = 1$	1500	Yes	268	0.457	0.246*	0.232	0.816*
$\lambda_P = 1$	4000	Yes	1224	0.891	0.148*	0.590	0.800*
$\lambda_P = 2$	1500	Yes	807	0.550	0.145*	0.373*	0.816*
$\lambda_P = 2$	4000	Yes	3773	0.872	0.119*	0.775*	0.820*
$\lambda_P = 3$	1500	Yes	1434	0.488	0.115*	0.421*	0.815*
$\lambda_P \approx 4.77 \text{ (OPTN)}$	1500	Yes	2652	0.537	0.103*	0.449	0.812

**Experimental Results.** We bold steady-state parameters  $\zeta > 0.8$ ,  ${\rm MAE}$  scores < 0.2, and  ${\rm IOU}$  scores > 0.5. We asterisk any federated learning experiments that improve relative performance.

#### Diagnosing Mechanism Behavior with SHAP



#### Visualizing Miscalibrations with SHAP + TSNE



We proposed a random-forest approach

	Old	Young
Large	O, W, Q	W, Q
Small	O, W, Q	Q

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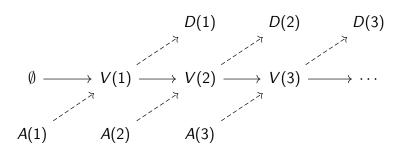
- **2** High values of  $\zeta$  give a proxy for success
- Our approach can be used to inform policy and make kidney exchanges more fair
- We developed a state-of-the-art simulator

#### **Exchange Dynamics**

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$$0(1) D(2) D(3)$$

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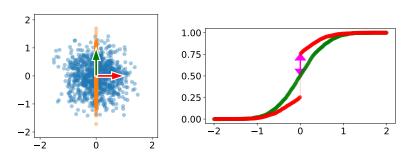
$$A(1) A(2) A(3)$$

Match record:

$$\mathcal{R}_{\mathcal{T}} = \left\{ (v, O(v), W(v), Q(v)) \mid v \in \bigcup_{t=1}^{\mathcal{T}} D(t) \right\}$$

#### Shifted Directions

We say that a unit vector  $\mathbf{z}$  is  $\delta$ -shifted if the Kolmogorov distance between the one-dimensional projections of the data onto  $\mathbf{z}$  is at least  $\delta$ :



We say that  $\mathcal{R}_T$  is  $(\gamma, \delta)$ -shifted if at least a  $\gamma$  fraction of all unit directions are  $\delta$ -shifted.

#### Distributional Shift and Steady-State Exchanges

Shift decreases as the age of the exchange increases, even controlling for the size of the dataset! But why?

D	REC_A	REC_B	DON_A	DON_B
1000	0.32	0.21	0.78	0.54
50000	0.22	0.15	0.78	0.48
Test	0.24	0.17	0.79	0.50

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It turns out that these two phenomena are in fact related!